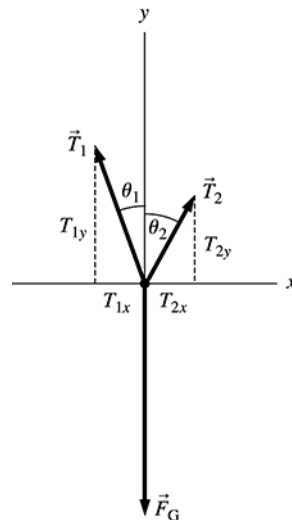


6.29. Model: You can model the beam as a particle in static equilibrium.

Visualize:

Pictorial representation



Known

$$m = 1000 \text{ kg}$$

$$T_{\text{max}} = 6000 \text{ N}$$

Find

$$\vec{T}_1 \text{ and } \vec{T}_2$$

Solve: Using Newton's first law, the equilibrium equations in vector and component form are:

$$\vec{F}_{\text{net}} = \vec{T}_1 + \vec{T}_2 + \vec{F}_G = \vec{0} \text{ N}$$

$$(F_{\text{net}})_x = T_{1x} + T_{2x} + F_{Gx} = 0 \text{ N}$$

$$(F_{\text{net}})_y = T_{1y} + T_{2y} + F_{Gy} = 0 \text{ N}$$

Using the free-body diagram yields:

$$-T_1 \sin \theta_1 + T_2 \sin \theta_2 = 0 \text{ N} \quad T_1 \cos \theta_1 + T_2 \cos \theta_2 - F_G = 0 \text{ N}$$

The mathematical model is reduced to a simple algebraic system of two equations with two unknowns, T_1 and T_2 . Substituting $\theta_1 = 20^\circ$, $\theta_2 = 30^\circ$, and $F_G = mg = 9800 \text{ N}$, the simultaneous equations become

$$-T_1 \sin 20^\circ + T_2 \sin 30^\circ = 0 \text{ N} \quad T_1 \cos 20^\circ + T_2 \cos 30^\circ = 9800 \text{ N}$$

You can solve this system of equations by simple substitution. The result is $T_1 = 6397 \text{ N}$ and $T_2 = 4376 \text{ N}$.

Assess: The above approach and result seem reasonable. Intuition indicates there is more tension in the left rope than in the right rope.